



Quadcopter Overview, Moment & Center of Gravity

October 15, 2018

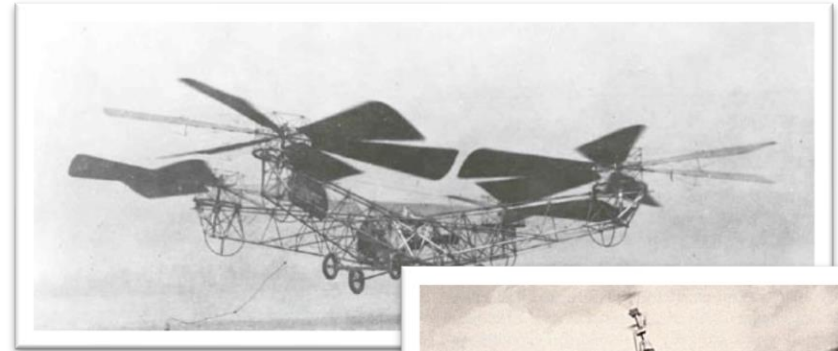
Quadcopter Overview

- Quadcopter
 - A multi-rotor helicopter that is lifted and propelled by four rotors.
 - Unmanned Aerial Vehicle (UAV)
 - Drones
- Characteristic
 - **Rotorcraft vs. Fixed Wing Aircraft**
 - Control of the vehicles motion is done **by altering the rotation rate** of one or more rotors at the same time, thus changing its torque load and thrust.
- Options
 - Remotely piloted
 - Autonomous (follow a fixed flight plan)



Quadcopter Overview

- History of Multirotor copter (piloted)
 - A solution to vertical flight
 - Counter-rotation and the relatively short blades for ease of construction.
 - Breguet-Richet Gyroplane (1907)
 - Oehmichen No.2 (1920)
 - de Bothezat helicopter (1922)
 - Convertawings Model A Quadrotor (1956)
 - Curtiss-Wright VZ-7 (1958)
 - Ehang 184 (2016)



Quadcopter Overview

- Early appearances in “Maker Faire”
- Commercial Usage
 - Aerial Photography and Video
 - Delivery
 - Entertainment
- Military Function
 - Surveillance
 - Search and Rescue
- Quadcopter Products
 - DJI
 - Phantom
 - Horizontal flight speed up to 52.5 ft/s
 - Vertical flight speed up to 16.4 ft/s
 - Parrot
 - Controlled by an App from tablet or mobile phone
 - Walkera
 - Hubscan



Quadcopter Overview

- Advancement in Technology
 - Wearable format
 - Drivable Quadcopter
 - Foldable Format



DJI Mavic



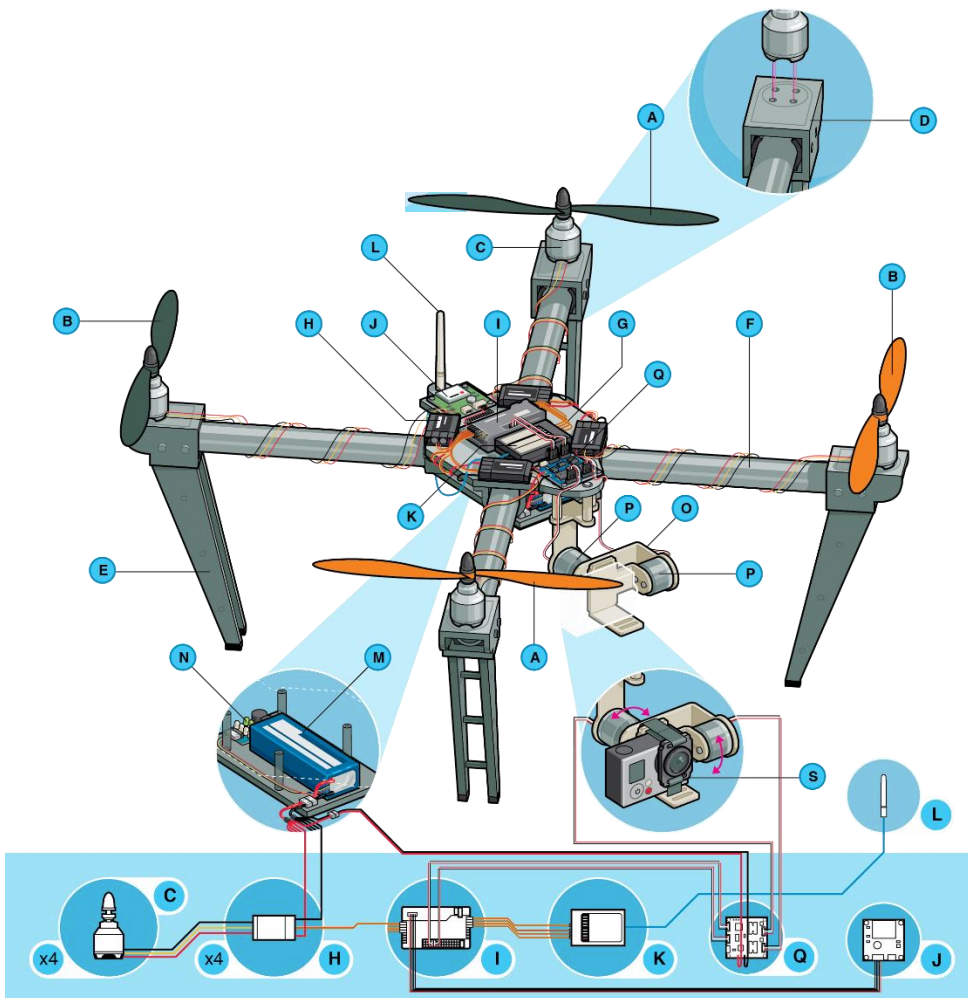
Nixie



Expandable drones
(various brands)

Quadcopter Overview

- Anatomy of Quadcopter



Propeller (Prop)

Motor

Motor Mount

Landing Gear

Boom

Main Body

Electronic Speed Controller (ESC)

Flight Controller

Receiver

Battery

Optional:

GPS Module

Antenna

Gimbal and Gimbal Motor

Camera

Moment

- Moment is the tendency of a force to twist or rotate an object.

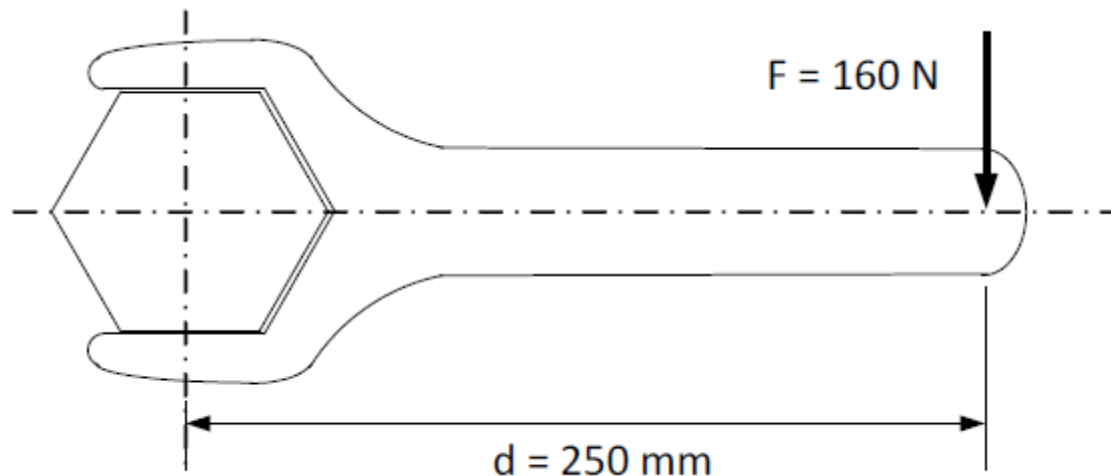
$$M = Fd$$

- F, force (N), $F=ma$ (m: mass, a: acceleration)
- d, distance between the location where the force is applied and a reference point (m)
- **Direction** of moment is demonstrated with right-hand rule.
 - Positive – Counter Clockwise motion
 - Negative – Clockwise motion
- For a balanced not spinning object, the moments of all forces should be equal to zero, $\sum M_i = 0$

Moment

- Moment is the tendency of a force to twist or rotate an object.

$$M = Fd$$

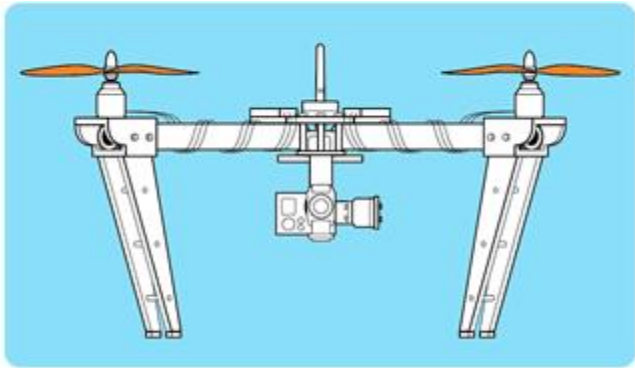


$$M = Fd = - (160\text{N})(0.25\text{m}) = - 40\text{Nm}$$

The rotation is clockwise in reference to the bolt

Quadcopter Overview

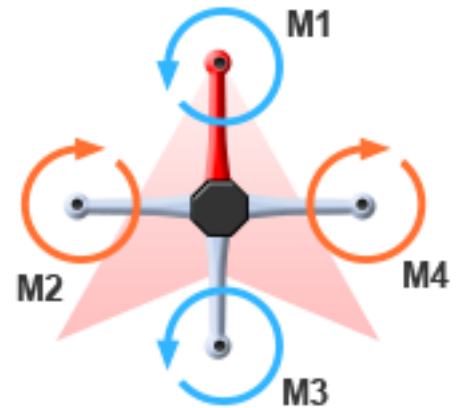
- Anatomy of Quadcopter
 - Examples: Side view of a quadcopter with camera system
 - Configurations



Side view



Top view with
a X Configuration



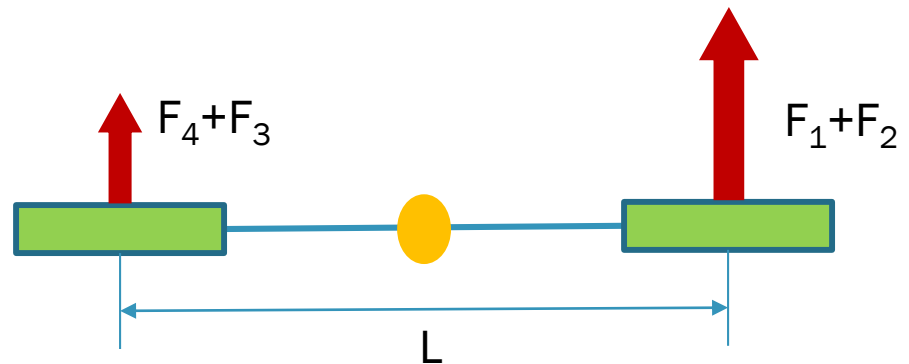
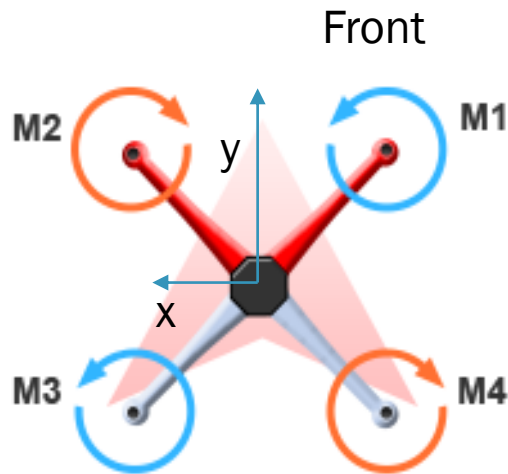
Top view with
a Cross or Plus Configuration

4 Rotors: 2 clockwise (CW) and 2 counter-clockwise (CCW)

Pitch

- Moment Produces Pitching

$$M = Fd$$



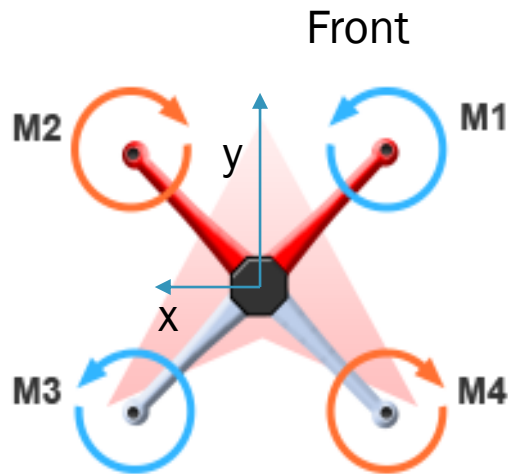
Increasing the speed on 1 and 2 Rotor

$$M_p = \sum M = (F_1 + F_2)\left(\frac{L}{2}\right) - (F_3 + F_4)\left(\frac{L}{2}\right)$$

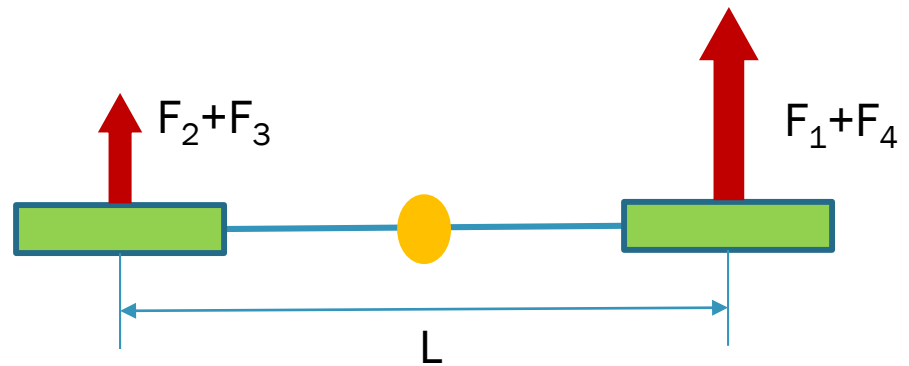
Roll

- Moment Produces Rolling

$$M = Fd$$



X Configuration



Side View

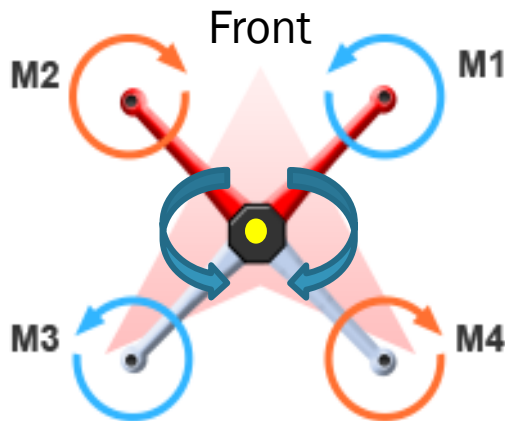
Increasing the speed on 1 and 4 Rotor

$$M_r = \sum M = (F_1 + F_4)\left(\frac{L}{2}\right) - (F_2 + F_3)\left(\frac{L}{2}\right)$$

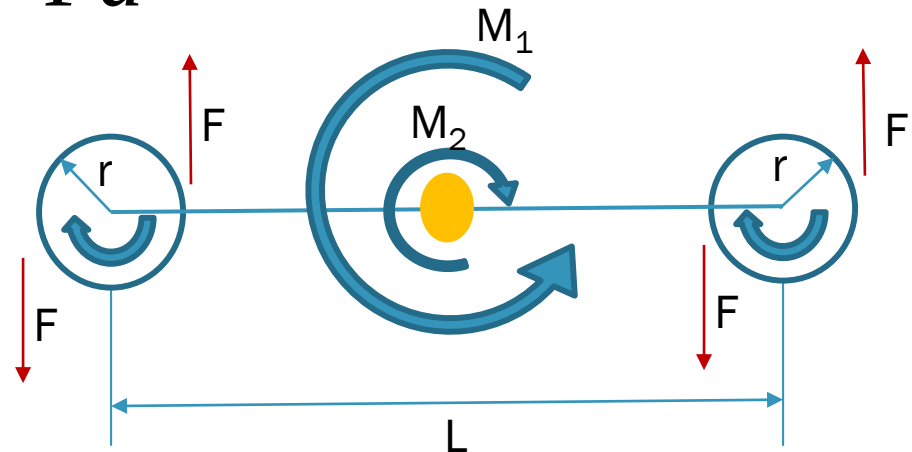
Yaw

- Moment Produces Yawing

$$M = Fd$$



X Configuration



Top View

Increasing the speed on 2 and 4 Rotor

$$M_y = \sum M = M_1 - M_2$$

$$M_1 = 2F\left(\frac{L}{2} + r\right)$$

$$M_2 = 2F\left(\frac{L}{2} - r\right)$$



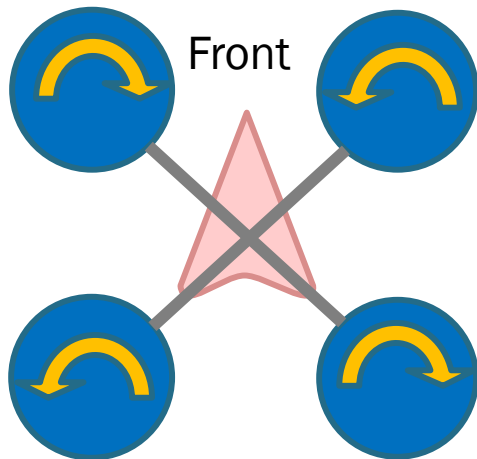
$$M_1 > M_2$$



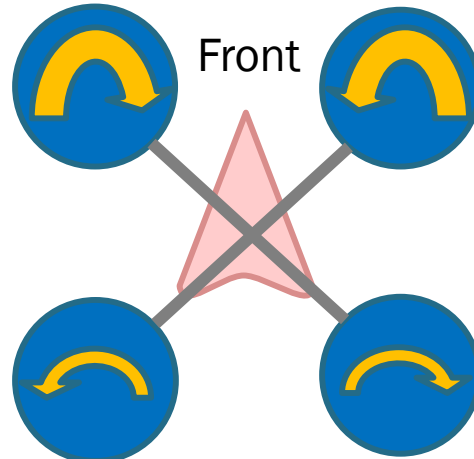
Counter Clockwise Rotation

Pitch, Roll, Yaw

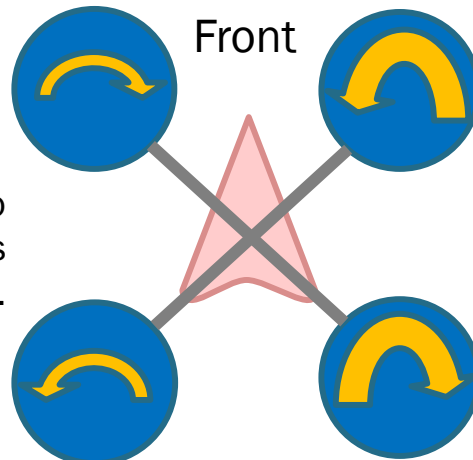
- Moment Produces Movements of the X Configured Quadcopter



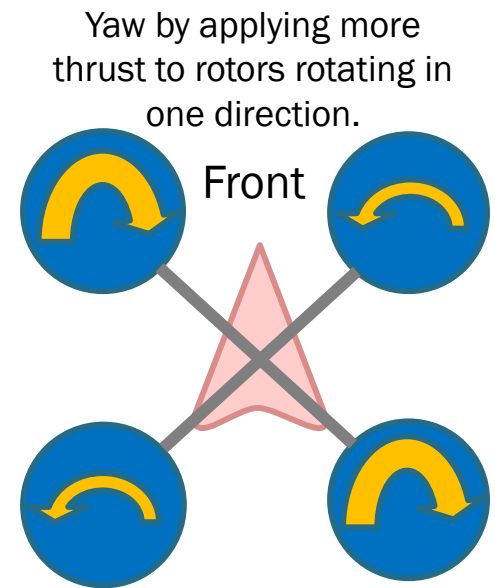
Adjusts its altitude by applying equal thrust to all four rotors.



Pitch by applying more thrust to two rotors and less thrust to its diametrically opposite rotors.



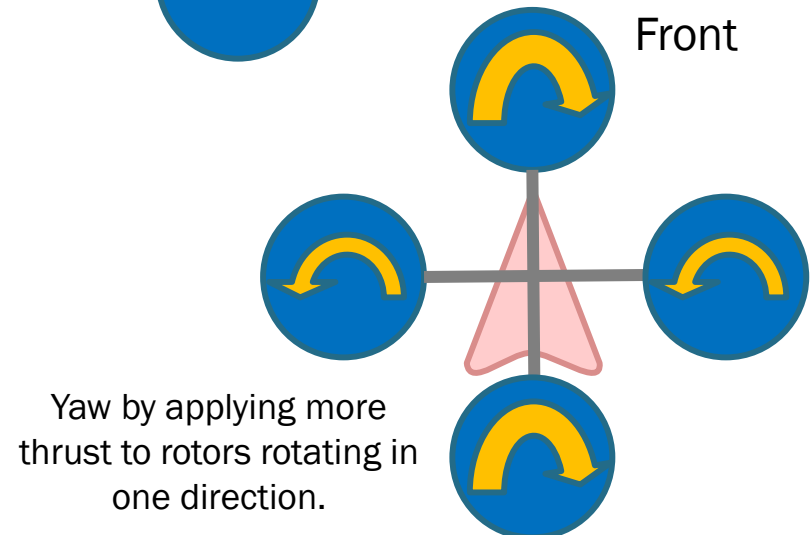
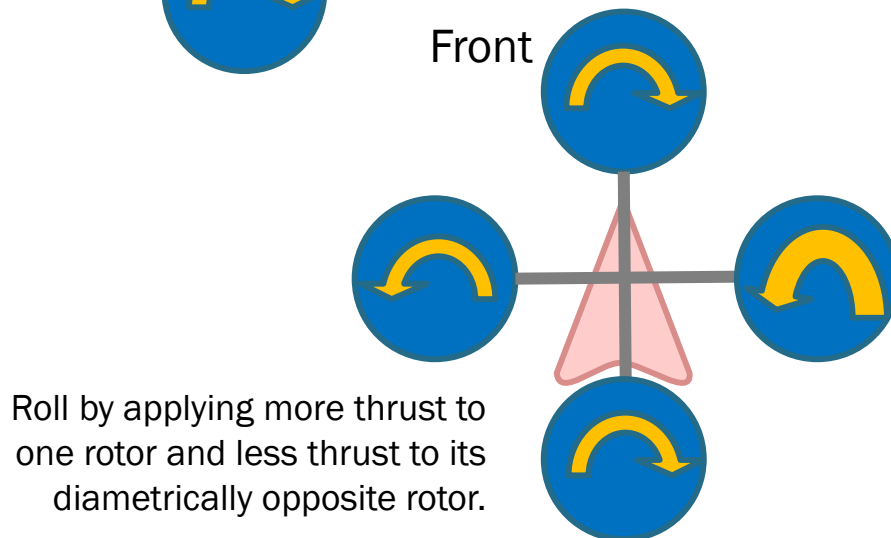
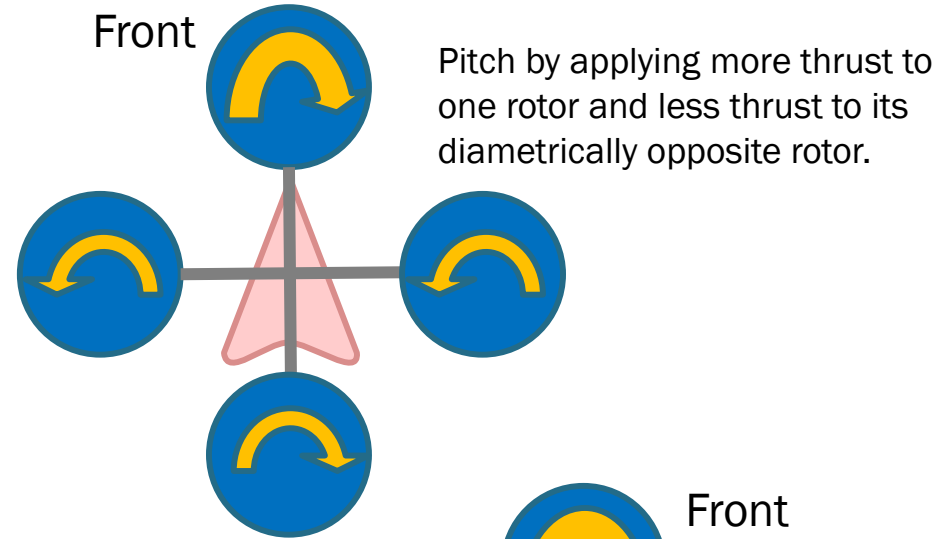
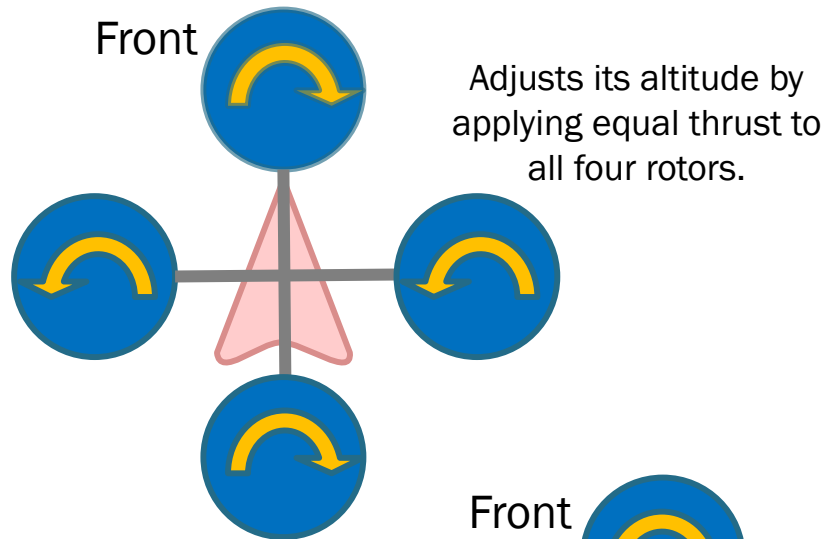
Roll by applying more thrust to two rotor and less thrust to its diametrically opposite rotors.



Yaw by applying more thrust to rotors rotating in one direction.

Pitch, Roll, Yaw

- Moment Produces Movements of the Plus Configured Quadcopter



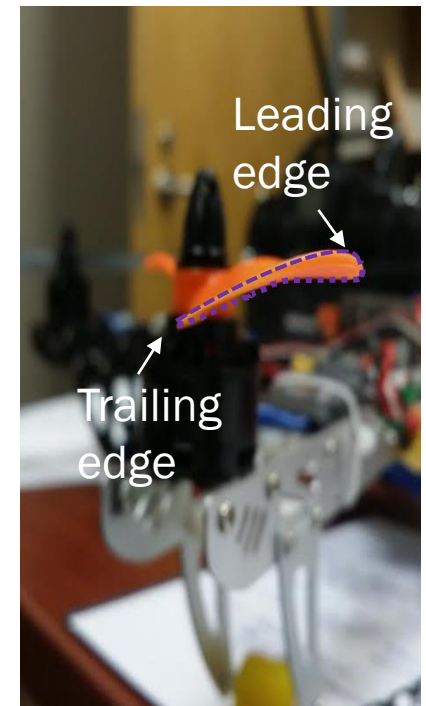
Quadcopter Overview

- Practical Tips on Propeller
 - How do you know whether the propeller is up or down?
 - Letters (writings) are on top
 - “Concave down”, side profile from the tip of the propeller



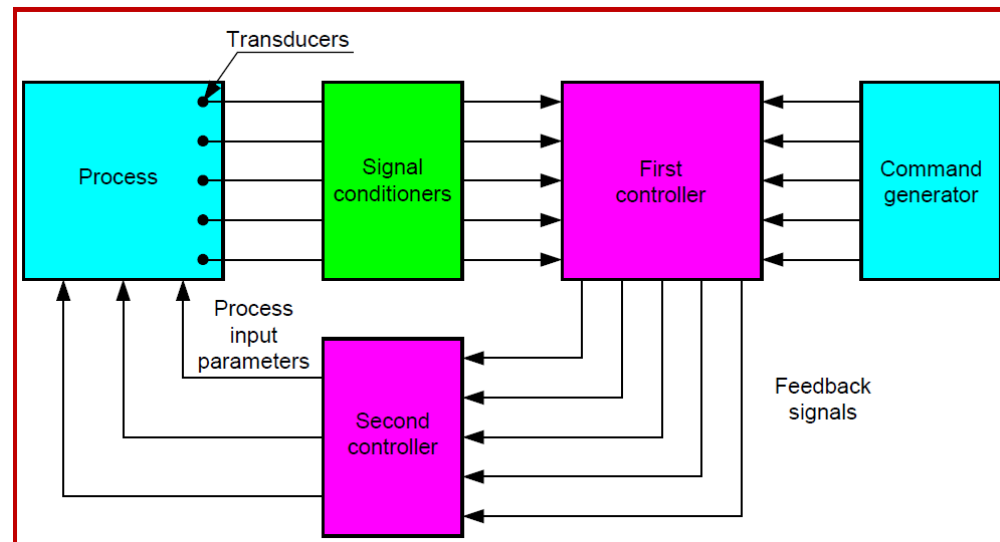
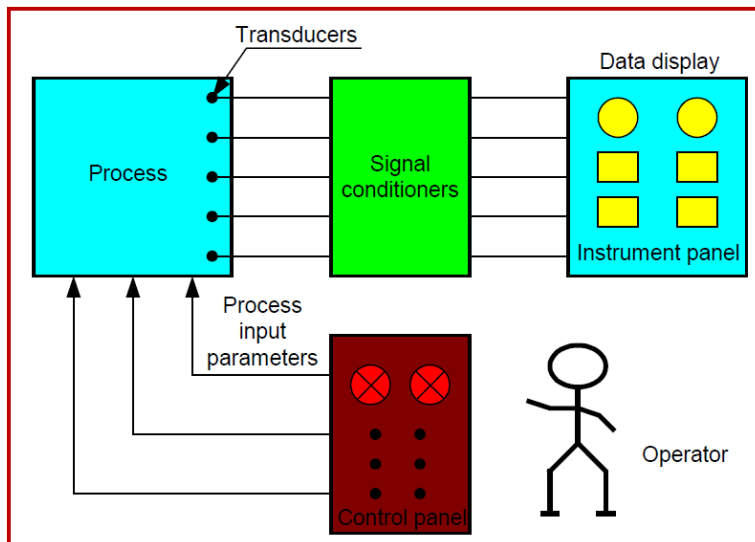
Quadcopter Overview

- Practical Tips on Propeller
 - Same design of propeller blades as a pair placed across from each other
 - Same color propellers often come as one clockwise and one counter-clockwise
 - Blade will turn toward the direction of leading edge of the airfoil



Control System

- Electronic Measurement systems are used in two types of process control
 - Open Loop Control (Manual, Remote Control)
 - Close Loop Control (Autonomous)



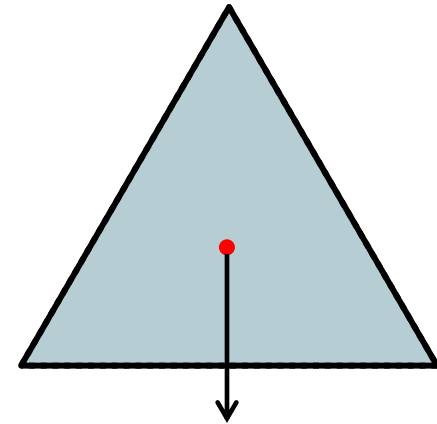
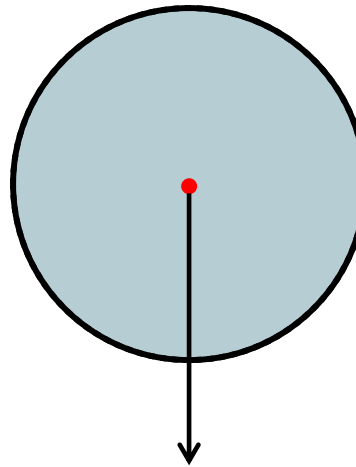
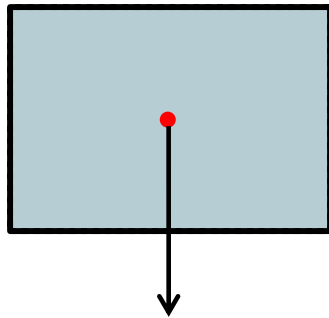
Quadcopter Overview

- Advancement in Technology
 - Quadcopters in Formation

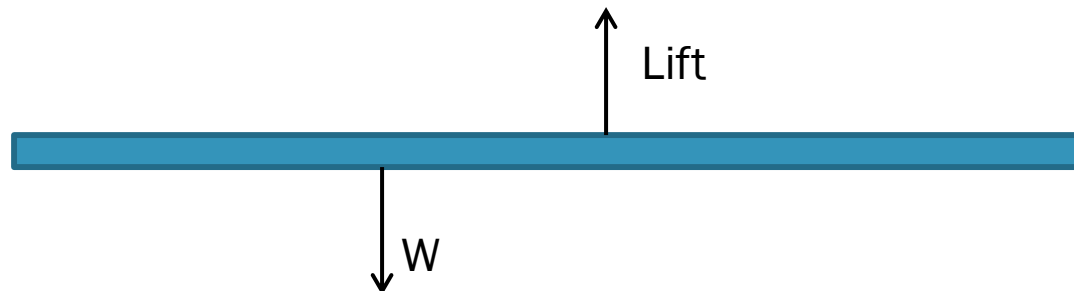


Center of Gravity (COG)

- Center of gravity is the weighted average location of all the mass in a body or group of bodies.



- The calculation of COG is important for Quadcopter design.



COG in Action

- Demo

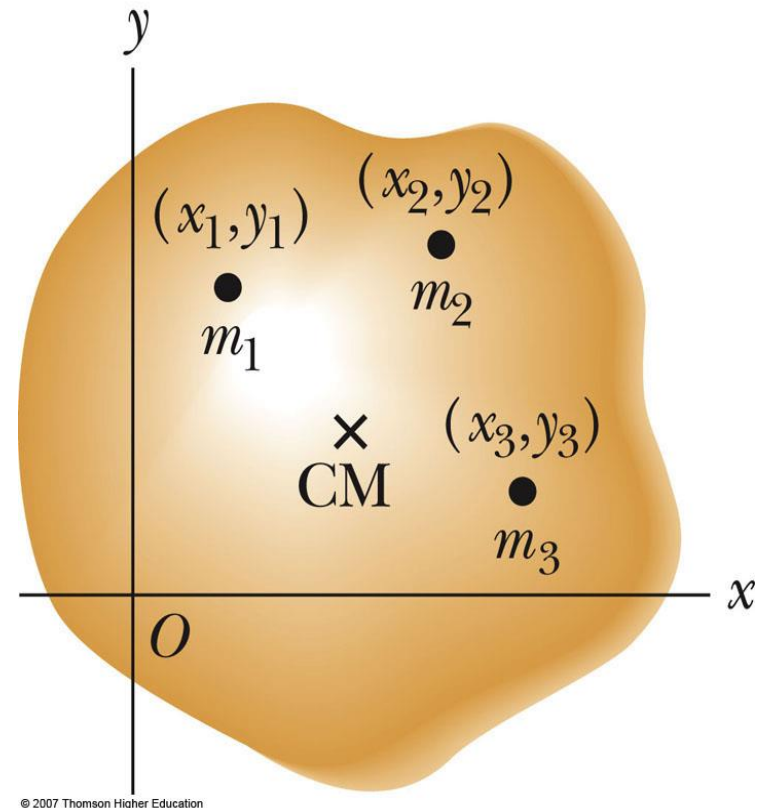


Center of Mass

- An object can be divided into many small particles
 - Each particle will have a specific mass and specific coordinates
- The **x** coordinate of the center of mass will be

$$x_{CM} = \frac{\sum_i m_i x_i}{\sum_i m_i}$$

- Similar expressions can be found for the **y** coordinates



COG Calculation

- All the **various** gravitational **forces** acting on all the various mass elements are **equivalent** to a **single** gravitational **force** acting through a **single point** called the center of gravity (**CoG**)

$$Mg_{CG}x_{CG} = (m_1 + m_2 + m_3 + \dots)g_{CG}x_{CG}$$

$$= m_1g_1x_1 + m_2g_2x_2 + m_3g_3x_3 + \dots$$

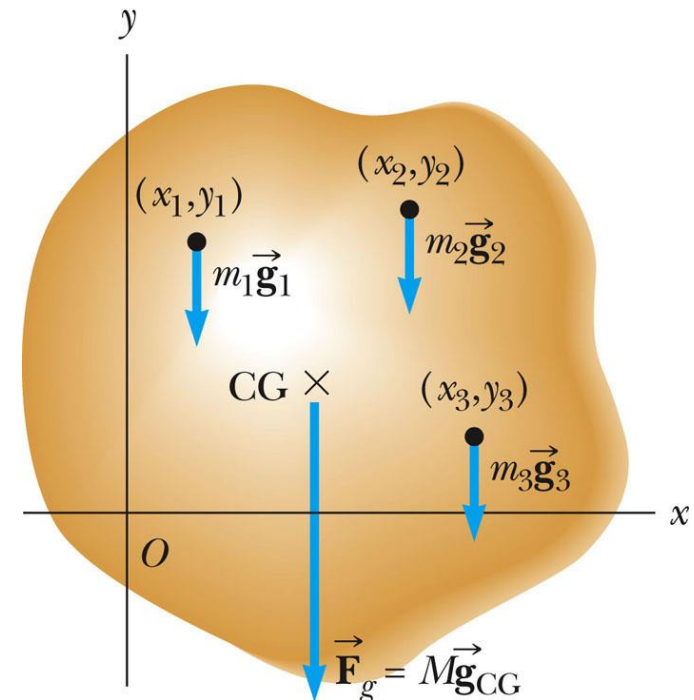
- If

$$g_1 = g_2 = g_3 = \dots$$

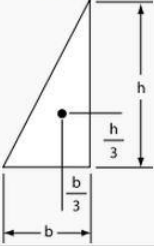
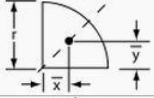
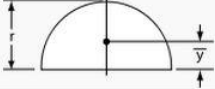
- then

$$x_{CG} = \frac{m_1x_1 + m_2x_2 + m_3x_3 + \dots}{m_1 + m_2 + m_3 + \dots} = \frac{\sum m_i x_i}{\sum m_i}$$

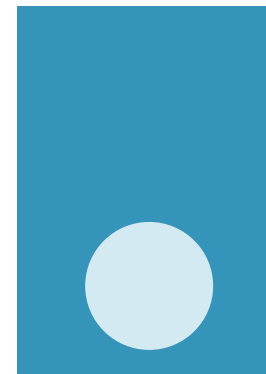
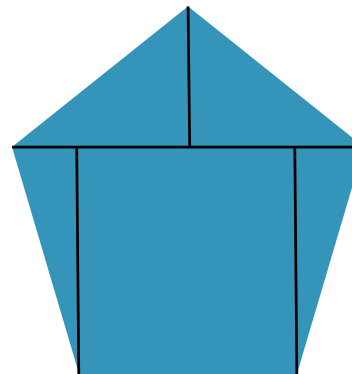
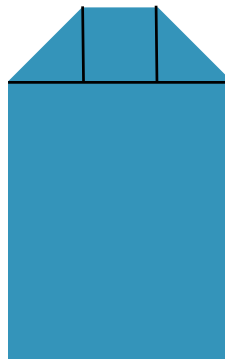
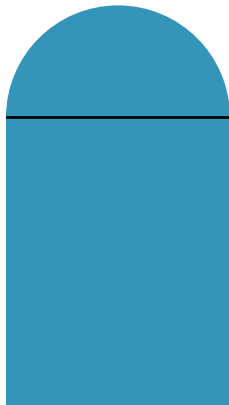
$$y_{CG} = \frac{m_1y_1 + m_2y_2 + m_3y_3 + \dots}{m_1 + m_2 + m_3 + \dots} = \frac{\sum m_i y_i}{\sum m_i}$$



COG in Action

Shape	Figure	$\bar{x}$	$\bar{y}$	Area
Right-triangular area		$-\frac{b}{3}$	$\frac{h}{3}$	$\frac{bh}{2}$
Quarter-circular area		$\frac{4r}{3\pi}$	$\frac{4r}{3\pi}$	$\frac{\pi r^2}{4}$
Semicircular area		0	$\frac{4r}{3\pi}$	$\frac{\pi r^2}{2}$

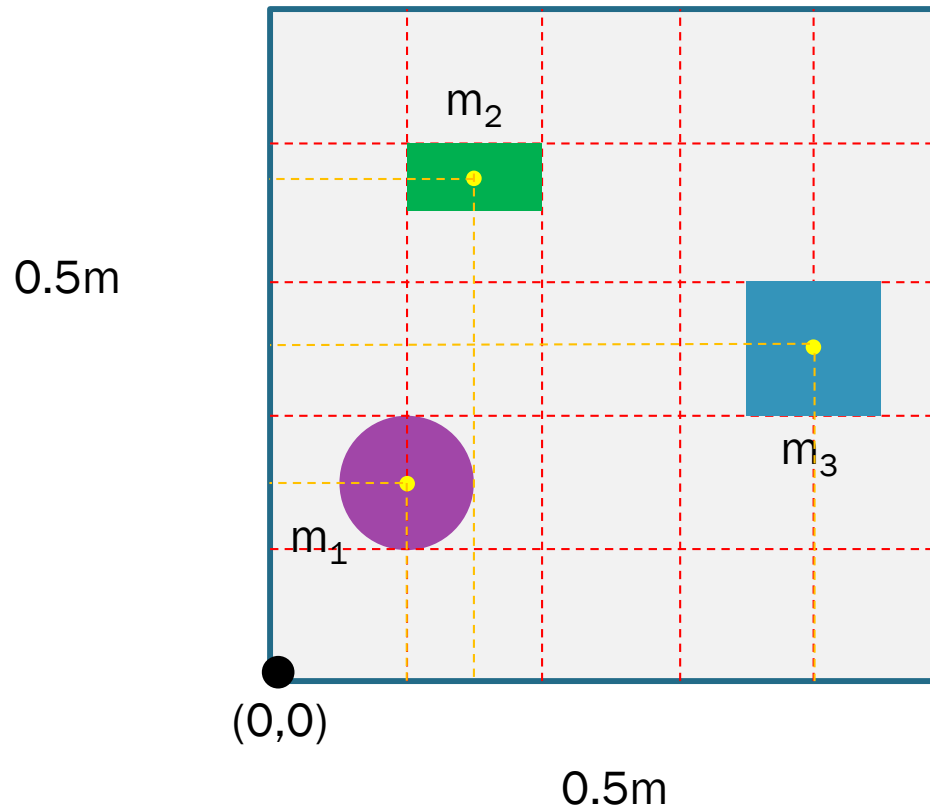
http://en.wikipedia.org/wiki/List_of_centroids



Divide complicated shapes into a combination of easy to calculate shapes

COG Example

- Find the x and y coordinators of the center of gravity on the following platform.



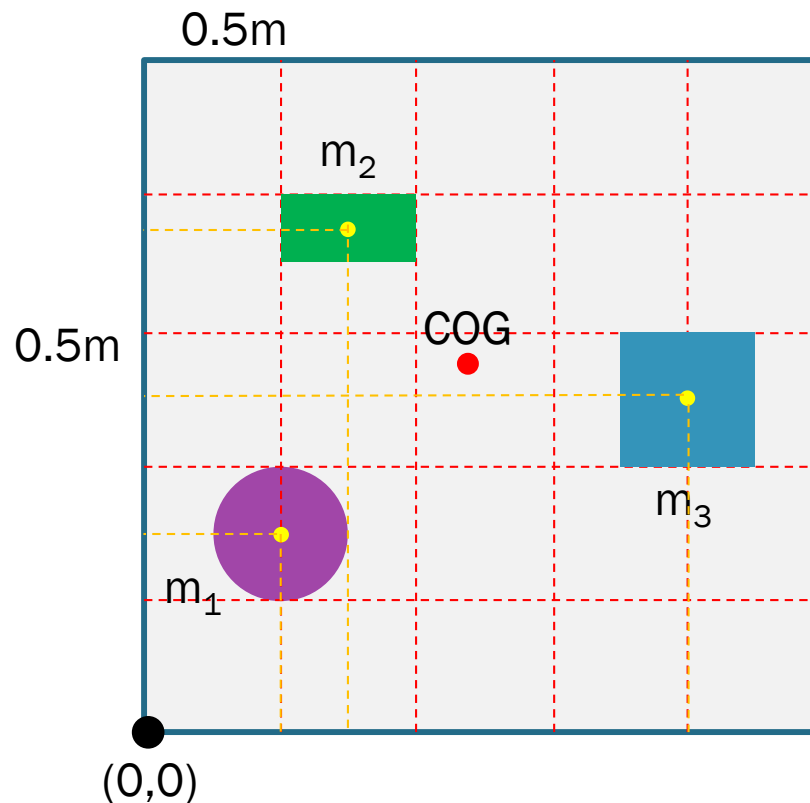
$$m_1 = 100 \text{ g}, d = 0.1\text{m}$$

$$m_2 = 200 \text{ g}$$
$$0.1\text{m} \times 0.05\text{m}$$

$$m_3 = 200 \text{ g}$$
$$0.1 \text{ m} \times 0.1\text{m}$$

COG Example

- Find the x and y coordinators of the center of gravity on the following platform.



$$m_1 = 100 \text{ g, } d = 0.1\text{m}; m_2 = 200 \text{ g, } 0.1\text{m} \times 0.05\text{m};$$

$$m_3 = 200 \text{ g, } 0.1 \text{ m} \times 0.1\text{m}$$

$$x_{CG} = \frac{\sum m_i x_i}{\sum m_i} = \frac{m_1 x_1 + m_2 x_2 + m_3 x_3}{m_1 + m_2 + m_3}$$

$$= \frac{100g(0.1\text{m}) + 200g(0.15\text{m}) + 200g(0.4\text{m})}{100g + 200g + 200g} = 0.24\text{m}$$

$$y_{CG} = \frac{\sum m_i y_i}{\sum m_i} = \frac{m_1 y_1 + m_2 y_2 + m_3 y_3}{m_1 + m_2 + m_3}$$

$$= \frac{100g(0.15\text{m}) + 200g(0.375\text{m}) + 200g(0.25\text{m})}{100g + 200g + 200g} = 0.28\text{m}$$

Reading Assignment for Week 3



“Introduction to Engineering Design” Book 11
Engineering Skills and Quadcopter Missions 4th Edition 2017

Chapter 6 “Dynamics and Control of Quadcopters”

Chapter 16 “Generation and Selection of Design Concepts”