# ICS FACULTY PANEL ON IMPROVING YOUR GRADUATE SCHOOL APPLICATION 

Wednesday, 18 Oct., 2017, 11:00am-12:50pm, in DBH-6011
**** Pizza, soft drinks, and refreshments will be served. ${ }^{* * * *}$

Wondering what to do to improve your graduate school application? Wondering how the process "really works," and what they look for? Come to this ICS FACULTY PANEL to hear advice from the ICS faculty.

The very people who admit students into the ICS graduate programs will give advice and answer questions about graduate school applications.

Next, a panel of current ICS graduate students will discuss their experiences in successfully navigating graduate school admission.

Sophomores, Juniors, and Masters students are especially encouraged to attend so that they can begin planning for graduate school now.

For students unable to attend the event, a video of the discussion subsequently will be posted on the ICS SAO web page.

# ICS FACULTY PANEL ON IMPROVING YOUR GRADUATE SCHOOL APPLICATION Wednesday, 18 Oct., 2017, 11:00am-12:50pm, in DBH-6011 

## **** Pizza, soft drinks, and refreshments will be served. ****

## Wondering what to do to improve your graduate school application? Come to this ICS FACULTY PANEL to hear advice from the ICS faculty.

Celina Mojica, Special Guest

* UCI Graduate Division

Dan Gillen, Professor and Chair, Statistics

* Statistics and Statistical Theory

Ian Harris, Professor and Vice Chair of Undergraduate Studies, Computer Science

* Computer Architecture and Design, Embedded Systems

Melissa Mazmanian, Professor and Vice Chair for Graduate Affairs, Informatics

* Communication technologies within organizational contexts, Identity projection in the digital age Gopi Meenakshisundaram, Professor and Associate Dean for Student Affairs, Computer Science
* Computer Graphics and Visualization, Computer Vision

Marios Papaefthymiou, Professor and Ted and Janice Smith Family Foundation Dean, Computer Science

* Computer Architecture and Design, Networks and Distributed Systems

André van der Hoek, Professor and Chair, Informatics

* Software Engineering

Zhaoxia Yu, Professor and Vice Chair of Undergraduate Affairs, Statistics

* Statistics and Statistical Theory

Following the faculty, a panel of current ICS graduate students will discuss their experiences in how they successfully navigated graduate school admission.

## Source: US Bureau of Labor Statistics

"Career Outlook, March 2016 / Data on display: Education matters" http://www.bls.gov/careeroutlook/2016/data-on-displayleducation-matters.htm

Earnings and unemployment rates by educational attainment, 2015


[^0]Professional degrees include MD, DDS, DVM, LLB, JD.
(Physicians, dentists, veterinarians, lawyers; the US has not offered the LLB since 1971.)

# Games and Adversarial Search 

CS171, Fall 2017<br>Introduction to Artificial Intelligence<br>Prof. Richard Lathrop



University of California

## Types of games

Deterministic:

## Chance:

## Perfect <br> Information: <br> Imperfect <br> Information:

| chess, checkers, go, <br> othello | backgammon, <br> monopoly |
| :--- | :--- |
| battleship, Kriegspiel | Bridge, poker, <br> scrabble, ... |

- Start with deterministic, perfect info games (easiest)
- Not considered:
- Physical games like tennis, ice hockey, etc.
- But, see "robot soccer", http://www.robocup.org/


## Typical assumptions

- Two agents, whose actions alternate
- Utility values for each agent are the opposite of the other
- "Zero-sum" game; this creates adversarial situation
- Fully observable environments
- In game theory terms:
- Deterministic, turn-taking, zero-sum, perfect information
- Generalizes: stochastic, multiplayer, non zero-sum, etc.
- Compare to e.g., Prisoner's Dilemma" (R\&N pp. 666-668)
- Non-turn-taking, Non-zero-sum, Imperfect information


## Game Tree (tic-tac-toe)

- All possible moves at each step

- How do we search this tree to find the optimal move?


## Search versus Games

- Search: no adversary
- Solution is (heuristic) method for finding goal
- Heuristics \& CSP techniques can find optimal solution
- Evaluation function: estimate cost from start to goal through a given node
- Examples: path planning, scheduling activities, ...
- Games: adversary
- Solution is a strategy
- Specifies move for every possible opponent reply
- Time limits force an approximate solution
- Evaluation function: evaluate "goodness" of game position
- Examples: chess, checkers, Othello, backgammon


## Games as search

- Two players, "MAX" and "MIN"
- MAX moves first, \& take turns until game is over
- Winner gets reward, loser gets penalty
- "Zero sum": sum of reward and penalty is constant
- Formal definition as a search problem:
- Initial state: set-up defined by rules, e.g., initial board for chess
- Player(s): which player has the move in state s
- Actions(s): set of legal moves in a state
- Results(s,a): transition model defines result of a move
- Terminal-Test(s): true if the game is finished; false otherwise
- Utility(s,p): the numerical value of terminal state s for player $p$
- E.g., win ( +1 ), lose ( -1 ), and draw ( 0 ) in tic-tac-toe
- E.g., win (+1), lose ( 0 ), and draw ( $1 / 2$ ) in chess
- MAX uses search tree to determine "best" next move


## Min-Max: an optimal procedure

- Designed to find the optimal strategy \& best move for MAX:

1. Generate the whole game tree to leaves
2. Apply utility (payoff) function to leaves
3. Back-up values from leaves toward the root:

- a Max node computes the max of its child values
- a Min node computes the min of its child values

4. At root: choose move leading to the child of highest value

## Two-ply Game Tree



Minimax maximizes the utility of the worst-case outcome for MAX

## Recursive min-max search

```
minMaxSearch(state)
Simple stub to call recursion f' ns
``` return argmax( [ minValue( apply(state,a) ) for each action a ] )
```

maxValue(state)
if (terminal(state)) return utility(state);
v = -infty
for each action a:
v = max( v, minValue( apply(state,a) ) )
return v
minValue(state)
if (terminal(state)) return utility(state);
v = infty
for each action a:
v = min( v, maxValue( apply(state,a) ) )
return v
v = -infty
for each action a:
v = max( v, minValue( apply(state,a) ) )
return v
minValue(state)
if (terminal(state)) return utility(state);
v = infty
for each action a:
$\mathrm{v}=\min (\mathrm{v}, \operatorname{maxValue}(\operatorname{apply}($ state, $a))$ )
return v

If recursion limit reached, eval position

Otherwise, find the worst child:

## Properties of minimax

- Complete? Yes (if tree is finite)
- Optimal?
- Yes (against an optimal opponent)
- Can it be beaten by a suboptimal opponent? (No - why?)
- Time? O(b
- Space?
- O(bm) (depth-first search, generate all actions at once)
- O(m) (backtracking search, generate actions one at a time)


## Game tree size

- Tic-tac-toe
$-B \approx 5$ legal actions per state on average; total 9 plies in game
- "ply" = one action by one player; "move" = two plies
$-5^{9}=1,953,125$
$-9!=362,880$ (computer goes first)
$-8!=40,320$ (computer goes second)
- Exact solution is quite reasonable
- Chess
$-b \approx 35$ (approximate average branching factor)
- d $\approx 100$ (depth of game tree for "typical" game)
$-b^{d}=35^{100} \approx 10^{154}$ nodes!!!
- Exact solution completely infeasible

It is usually impossible to develop the whole search tree.

## Cutting off search

- One solution: cut off tree before game ends
- Replace
- Terminal(s) with Cutoff(s) - e.g., stop at some max depth
- Utility(s,p) with Eval(s,p) - estimate position quality
- Does it work in practice?
$-b^{m} \approx 10^{6}, b \approx 35 \rightarrow m \approx 4$
- 4-ply look-ahead is a poor chess player
- 4-ply $\approx$ human novice
- 8-ply $\approx$ typical PC, human master
- 12-ply $\approx$ Deep Blue, human grand champion Kasparov
$-35^{12} \approx 10^{18}$ (Yikes! but possible, with other clever methods)


## Static (Heuristic) Evaluation Functions

- An Evaluation Function:
- Estimate how good the current board configuration is for a player.
- Typically, evaluate how good it is for the player, and how good it is for the opponent, and subtract the opponent's score from the player's.
- Often called "static" because it is called on a static board position
- Ex: Othello: Number of white pieces - Number of black pieces
- Ex: Chess: Value of all white pieces - Value of all black pieces
- Typical value ranges:

$$
[-1,1] \text { (loss/win) or }[-1,+1] \text { or }[0,1]
$$

- Board evaluation: X for one player => -X for opponent
- Zero-sum game: scores sum to a constant


## Evaluation functions



For chess, typically linear weighted sum of features

$$
\operatorname{Eval}(s)=w_{1} f_{1}(s)+w_{2} f_{2}(s)+\ldots+w_{n} f_{n}(s)
$$

e.g., $w_{1}=9$ with
$f_{1}(s)=$ (number of white queens) - (number of black queens), etc.

## Applying minimax to tic-tac-toe

- The static heuristic evaluation function:
- Count the number of possible win lines



X has 6
possible win paths

$X$ has 4 possible wins $O$ has 6 possible wins

$$
E(n)=4-6=-2
$$

$$
E(n)=5-4=1
$$

$$
E(s)=6-5=1
$$

## Minimax values (two ply)



Figure 4.17 Two-ply minimax applied to the opening move of tic-tac-toe.

## Minimax values (two ply)



Figure 4.18 Two-ply minimax applied to $X$ 's second move of tic-tac-toe.

## Minimax values (two ply)



Figure 4.19 Two-ply minimax applied to $X$ 's move near end game.

## Digression: Exact values don't matter

MAX

MIN


Behaviour is preserved under any monotonic transformation of Eval
Only the order matters:
payoff in deterministic games acts as an ordinal utility function

## Iterative deepening

- In real games, there is usually a time limit T to make a move
- How do we take this into account?
- Minimax cannot use "partial" results with any confidence, unless the full tree has been searched
- Conservative: set small depth limit to guarantee finding a move in time < T
- But, we may finish early - could do more search!
- In practice, iterative deepening search (IDS) is used
- IDS: depth-first search with increasing depth limit
- When time runs out, use the solution from previous depth
- With alpha-beta pruning (next), we can sort the nodes based on values from the previous depth limit in order to maximize pruning during the next depth limit => search deeper!


## Limited horizon effects

- The Horizon Effect
- Sometimes there's a major "effect" (such as a piece being captured) which is just "below" the depth to which the tree has been expanded.
- The computer cannot see that this major event could happen because it has a "limited horizon".
- There are heuristics to try to follow certain branches more deeply to detect such important events
- This helps to avoid catastrophic losses due to "short-sightedness"
- Heuristics for Tree Exploration
- Often better to explore some branches more deeply in the allotted time
- Various heuristics exist to identify "promising" branches
- Stop at "quiescent" positions - all battles are over, things are quiet
- Continue when things are in violent flux - the middle of a battle


## Selectively deeper game trees



## Eliminate redundant nodes

- On average, each board position appears in the search tree approximately $10^{150} / 10^{40} \approx 10^{100}$ times
- Vastly redundant search effort
- Can't remember all nodes (too many)
- Can't eliminate all redundant nodes
- Some short move sequences provably lead to a redundant position
- These can be deleted dynamically with no memory cost
- Example:

1. P-QR4 P-QR4; 2. P-KR4 P-KR4
leads to the same position as
2. P-QR4 P-KR4; 2. P-KR4 P-QR4

## Summary

Game playing as a search problem

- Game trees represent alternate computer / opponent moves
- Minimax: choose moves by assuming the opponent will always choose the move that is best for them
- Avoids all worst-case outcomes for Max, to find the best
- If opponent makes an error, Minimax will take optimal advantage (after) \& make the best possible play that exploits the error
- Cutting off search
- In general, it's infeasible to search the entire game tree
- In practice, Cutoff-Test decides when to stop searching
- Prefer to stop at quiescent positions
- Prefer to keep searching in positions that are still in flux
- Static heuristic evaluation function
- Estimate the quality of a given board configuration for MAX player
- Called when search is cut off, to determine value of position found


## Games \& Adversarial Search: Alpha-Beta Pruning

CS171, Fall 2017<br>Introduction to Artificial Intelligence<br>Prof. Richard Lathrop



## Alpha-Beta pruning <br> - Exploit the "fact" of an adversary

- If a position is provably bad
- It's no use searching to find out just how bad
- If the adversary can force a bad position
- It's no use searching to find the good positions the adversary won't let you achieve
- Bad = not better than we can get elsewhere


## Pruning with Alpha/Beta



Figure 4.17 Two-ply minimax applied to the opening move of tic-tac-toe.

## Alpha-Beta Example

Initially, possibilities are unknown: range ( $\alpha=-00, \beta=+\infty 0$ ) Do a depth-first search to the first leaf.


## Alpha-Beta Example

See the first leaf, after MIN's move: MIN updates $\beta$


## Alpha-Beta Example

See remaining leaves; value is known
Pass outcome to caller; MAX updates $\alpha$


## Alpha-Beta Example

Continue depth-first search to next leaf.
Pass $\alpha, \beta$ to descendants


## Alpha-Beta Example

Observe leaf value; MIN's level; MIN updates $\beta$
Prune - play will never reach the other nodes!


## Alpha-Beta Example

Pass outcome to caller \& update caller:


## Alpha-Beta Example

Continue depth-first exploration...
No pruning here; value is not resolved until final leaf.


## Alpha-Beta Example

Value at the root is resolved.


## General alpha-beta pruning

- Consider a node n in the tree:
- If player has a better choice at
- Parent node of $n$
- Or, any choice further up!
- Then n is never reached in play

- So:
- When that much is known about $n$, it can be pruned


## Recursive $\alpha-\beta$ pruning

```
abSearch(state)
    alpha, beta, a = -infty, +infty, None
    for each action a:
        alpha, a = max( (alpha,a) , (minValue( apply(state,a), alpha, beta), a) )
    return a
```

Simple stub to call recursion f' ns
Initialize alpha, beta; no move found
Score each action; update alpha \& best action

```
alpha, \(a=\max ((\) alpha, \(a),(\) minValue ( apply(state,a), alpha, beta), a) )
return a
```

If recursion limit reached, eval heuristic
Otherwise, find our best child:
If our options are too good, our min
ancestor will never let us come this way
Otherwise return the best we can find

```
minValue(state, al, be)
    if (cutoff(state)) return eval(state);
    for each action a:
    be = min(be, maxValue( apply(state,a), al, be)
            if (al, be) return -infty
    return be
```

```
maxValue(state, al, be)
    if (cutoff(state)) return eval(state);
    for each action a:
        al = max( al, minValue( apply(state,a), al, be)
        if (al, be) return +infty
    return al
```

If recursion limit reached, eval heuristic
Otherwise, find the worst child:
If our options are too bad, our max
ancestor will never let us come this way
Otherwise return the worst we can find

## Effectiveness of $\alpha-\beta$ Search

- Worst-Case
- Branches are ordered so that no pruning takes place. In this case alpha-beta gives no improvement over exhaustive search
- Best-Case
- Each player' s best move is the left-most alternative (i.e., evaluated first)
- In practice, performance is closer to best rather than worst-case
- In practice often get $O\left(b^{(d / 2)}\right)$ rather than $O\left(b^{d}\right)$
- This is the same as having a branching factor of sqrt(b),
- since $(s q r t(b))^{d}=b^{(d / 2)}$ (i.e., we have effectively gone from $b$ to square root of $b$ )
- In chess go from $b^{\sim} 35$ to $b \sim 6$
- permiting much deeper search in the same amount of time


## Iterative deepening

- In real games, there is usually a time limit T to make a move
- How do we take this into account?
- Minimax cannot use "partial" results with any confidence, unless the full tree has been searched
- Conservative: set small depth limit to guarantee finding a move in time < T
- But, we may finish early - could do more search!
- Added benefit with Alpha-Beta Pruning:
- Remember node values found at the previous depth limit
- Sort current nodes so that each player's best move is left-most child
- Likely to yield good Alpha-Beta Pruning => better, faster search
- Only a heuristic: node values will change with the deeper search
- Usually works well in practice


## Comments on alpha-beta pruning

- Pruning does not affect final results
- Entire subtrees can be pruned
- Good move ordering improves pruning
- Order nodes so player's best moves are checked first
- Repeated states are still possible
- Store them in memory = transposition table


## Iterative deepening reordering

Which leaves can be pruned?
None!
because the most favorable nodes are explored last...


## Iterative deepening reordering

Different exploration order: now which leaves can be pruned?

## Lots!

because the most favorable nodes are explored first!


## Iterative deepening reordering

Order with no pruning; use iterative deepening approach. Assume node score is the average of leaf values below.


## Iterative deepening reordering

Order with no pruning; use iterative deepening approach. Assume node score is the average of leaf values below.

For L=2,
switch the order of these nodes!


MAX

MIN

## Iterative deepening reordering

Order with no pruning; use iterative deepening approach. Assume node score is the average of leaf values below.

For L=2,
switch the order of these nodes!


MAX

MIN

## Iterative deepening reordering

Order with no pruning; use iterative deepening approach.
Assume node score is the average of leaf values below.

Alpha-Beta pruning would prune this node at $\mathrm{L}=2$

For $\mathrm{L}=3$, switch the order of these nodes!


## Iterative deepening reordering

Order with no pruning; use iterative deepening approach.
Assume node score is the average of leaf values below.

Alpha-Beta pruning would prune this node at $\mathrm{L}=2$

For $\mathrm{L}=3$, switch the order of these nodes!


## Iterative deepening reordering

Order with no pruning; use iterative deepening approach. Assume node score is the average of leaf values below.

Lots of pruning!
The most favorable nodes are explored earlier.


MAX

MIN

## Longer Alpha-Beta Example

Branch nodes are labelel A..K for easy discussion
$\alpha, \beta$, initial values $\longrightarrow \alpha=-\infty$ $\beta=+\infty \bigwedge \operatorname{MAX}$

| 4 | 5 | 6 | 6 | 1 | 9 | 5 | 4 | 1 | 3 | 2 | 6 | 1 | 3 | 6 | 8 | 6 | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## Longer Alpha-Beta Example

Note that cut-off occurs at different depths...
$\alpha=-\infty$
current $\alpha, \beta$,
passed to kids


## Longer Alpha-Beta Example



We also are running MiniMax search and recording node values within the triangles, without explicit comment.

## Longer Alpha-Beta Example



## Longer Alpha-Beta Example



## Longer Alpha-Beta Example



## Longer Alpha-Beta Example



## Longer Alpha-Beta Example



## Longer Alpha-Beta Example



## Longer Alpha-Beta Example

return node value,

$$
\alpha=-\infty
$$

MIN updates $\beta$,
no change to $\beta$

$\Downarrow$| $\alpha=-\infty$ |
| :--- |
| $\beta=6$ |

kid=A

## Longer Alpha-Beta Example

see next leaf,
MIN updates $\beta$, no change to $\beta$


## Longer Alpha-Beta Example

return node value, $\longrightarrow \alpha=6$
MAX updates $\alpha$


## Longer Alpha-Beta Example



## Longer Alpha-Beta Example



## Longer Alpha-Beta Example



## Longer Alpha-Beta Example



## Longer Alpha-Beta Example



Note that we never find out, what is the node value of H? But we have proven it doesn't matter, so we don't care.

## Longer Alpha-Beta Example

return node value, $\longrightarrow \alpha=6$
MAX updates $\alpha, \quad \beta=+\infty$


## Longer Alpha-Beta Example

current $\alpha, \beta$,
passed to kid=C
$\alpha=6$
$\beta=+\infty$
kid $=C$

$$
\begin{aligned}
& \alpha=6 \\
& \beta=+\infty
\end{aligned}
$$

## Longer Alpha-Beta Example

see first leaf,
MIN updates $\beta$
$\alpha=6$
$\beta=9$


## Longer Alpha-Beta Example



## Longer Alpha-Beta Example



## Longer Alpha-Beta Example



## Longer Alpha-Beta Example



## Longer Alpha-Beta Example



## Longer Alpha-Beta Example

return node value, $\longrightarrow \alpha=6$
MAX updates $\alpha, \quad \beta=+\infty$


## Longer Alpha-Beta Example

current $\alpha, \beta$, passed to kid=D
$\alpha=6$
$\alpha=6$
$\beta=+\infty$
kid=D


## Longer Alpha-Beta Example

see first leaf,
MIN updates $\beta$
$\alpha=6$
$\beta=6$


## Longer Alpha-Beta Example



## Alpha-Beta Example \#2



## Alpha-Beta Example \#2

MAX moves to $A$,


## Nondeterministic games

- Ex: Backgammon
- Roll dice to determine how far to move (random)
- Player selects which checkers to move (strategy)



## Nondeterministic games

- Chance (random effects) due to dice, card shuffle, ...
- Chance nodes: expectation (weighted average) of successors
- Simplified example: coin flips



## Pruning in nondeterministic games

- Can still apply a form of alpha-beta pruning


MAX

Chance

MIN

## Pruning in nondeterministic games

- Can still apply a form of alpha-beta pruning


MAX

Chance

## Pruning in nondeterministic games

- Can still apply a form of alpha-beta pruning


MAX

Chance

## Pruning in nondeterministic games

- Can still apply a form of alpha-beta pruning


MAX

Chance

## Pruning in nondeterministic games

- Can still apply a form of alpha-beta pruning


MAX

Chance

## Pruning in nondeterministic games

- Can still apply a form of alpha-beta pruning


MAX

Chance

## Pruning in nondeterministic games

- Can still apply a form of alpha-beta pruning


MAX

Chance

## Pruning in nondeterministic games

- Can still apply a form of alpha-beta pruning


MAX

Chance

## Pruning in nondeterministic games

- Can still apply a form of alpha-beta pruning



## Partially observable games

- R\&N Chapter 5.6 - "The fog of war"
- Background: R\&N, Chapter 4.3-4
- Searching with Nondeterministic Actions/Partial Observations
- Search through Belief States (see Fig. 4.14)
- Agent's current belief about which states it might be in, given the sequence of actions \& percepts to that point
- Actions(b) = ?? Union? Intersection?
- Tricky: an action legal in one state may be illegal in another
- Is an illegal action a NO-OP? or the end of the world?
- Transition Model:
$-\operatorname{Result}(b, a)=\left\{s^{\prime}: s^{\prime}=\operatorname{Result}(s, a)\right.$ and $s$ is a state in $\left.b\right\}$
- Goaltest(b) = every state in b is a goal state


## Belief States for Unobservable Vacuum World



## Partially observable games

- R\&N Chapter 5.6
- Player's current node is a belief state
- Player's move (action) generates child belief state
- Opponent's move is replaced by Percepts(s)
- Each possible percept leads to the belief state that is consistent with that percept
- Strategy = a move for every possible percept sequence
- Minimax returns the worst state in the belief state
- Many more complications and possibilities!!
- Opponent may select a move that is not optimal, but instead minimizes the information transmitted, or confuses the opponent
- May not be reasonable to consider ALL moves; open P-QR3??
- See R\&N, Chapter 5.6, for more info


## The State of Play

- Checkers:
- Chinook ended 40-year-reign of human world champion Marion Tinsley in 1994.
- Chess:
- Deep Blue defeated human world champion Garry Kasparov in a six-game match in 1997.
- Othello:
- human champions refuse to compete against computers: they are too good.
- Go:
- AlphaGo recently (3/2016) beat $9^{\text {th }}$ dan Lee Sedol
- b>300 (!); full game tree has > 10^760 leaf nodes (!!)
- See (e.g.) http://www.cs.ualberta.ca/~games/ for more info


## High branching factors

- What can we do when the search tree is too large?
- Ex: Go ( $b=50-200+$ moves per state)
- Heuristic state evaluation (score a partial game)
- Where does this heuristic come from?
- Hand designed
- Machine learning on historical game patterns
- Monte Carlo methods - play random games



## Monte Carlo heuristic scoring

- Idea: play out the game randomly, and use the results as a score
- Easy to generate \& score lots of random games
- May use 1000s of games for a node
- The basis of Monte Carlo tree search algorithms...



## Monte Carlo Tree Search

- Should we explore the whole (top of) the tree?
- Some moves are obviously not good...
- Should spend time exploring / scoring promising ones
- This is a multi-armed bandit problem:
- Want to spend our time on good moves
- Which moves have high payout?
- Hard to tell - random...
- Explore vs. exploit tradeoff



## Visualizing MCTS

- At each level of the tree, keep track of
- Number of times we' ve explored a path
- Number of times we won
- Follow winning (from max/min perspective) strategies more often, but also explore others



## Summary

- Game playing is best modeled as a search problem
- Game trees represent alternate computer/opponent moves
- Evaluation functions estimate the quality of a given board configuration for the Max player.
- Minimax is a procedure which chooses moves by assuming that the opponent will always choose the move which is best for them
- Alpha-Beta is a procedure which can prune large parts of the search tree and allow search to go deeper
- For many well-known games, computer algorithms based on heuristic search match or out-perform human world experts.


[^0]:    Note: Data are for persons age 25 and over. Earnings are for full-time wage and salary workers.
    Source: U.S. Bureau of Labor Statistics, Current Population Survey

