

3A: Extra exercises 2

Remark: the exercise below will be graded carefully. Give explanations and computations.

Exercise 1

Consider the matrix $A = \begin{bmatrix} 1 & 2 & 1 & 1 & 1 \\ 3 & 6 & 0 & 3 & 1 \\ 2 & 4 & 2 & 1 & 1 \end{bmatrix}$ and vector $\mathbf{b} = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$. Finally, consider the vector

$$\mathbf{c} = \begin{bmatrix} 1 \\ -1 \\ 2 \\ 1 \\ 3 \end{bmatrix}.$$

a) Compute $A\mathbf{c}$.

b) Find the solution(s) of the equation

$$A\mathbf{x} = \mathbf{b}$$

in parametric vector form.

c) Find the solution(s) of the equation

$$A\mathbf{x} = \mathbf{0}$$

in parametric vector form.

d) Determine whether the first, second and fourth columns of A are linearly independent or not.