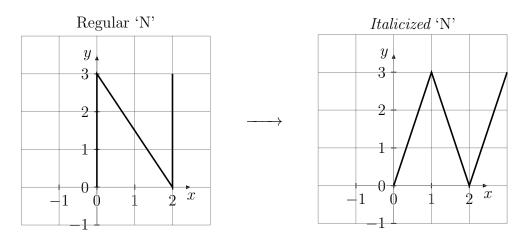
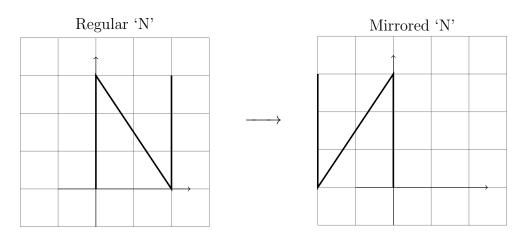
Opening Question: You are a graphic designer developing a new font. Your current task is to italicize the letter 'N'. If you draw 'N' in  $\mathbb{R}^2$ , can you create a function to italicize it? Is your function a linear transformation? Will it work for other letters?

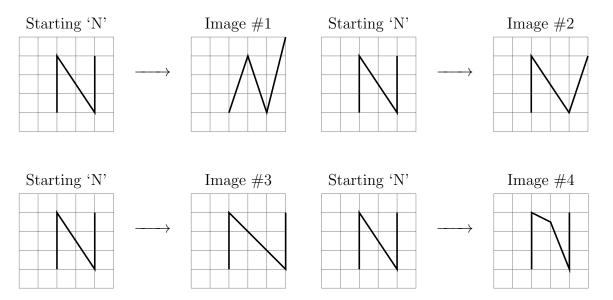
1. You draw the letter 'N' in  $\mathbb{R}^2$  and then transform it into *italics*. Viewing each point on the 'N' as a vector in  $\mathbb{R}^2$ , can you find a linear transformation that moves the vectors to the *italicized* positions?



2. Next, you want to take a mirror image of your characters (see below). Using the same approach as before, can you find a linear transformation that does this?



- 3. Reflect back on #1 and #2 and answer the following questions:
  - (a) How do you build the standard matrix of a linear transformation?
  - (b) What is the least amount of information we need about what T does to vectors in  $\mathbb{R}^n$  before we know what T does to all vectors in  $\mathbb{R}^n$ ?
- 4. Now, consider the following transformations of the letter 'N'. Which are not possible to achieve by a linear transformation? Change the image as little as possible so that it is the result of a linear transformation.



5. Go further:

- (a) What happens when you *italicize* then mirror? What about doing it in the other order?
- (b) If you had a linear transformation from  $\mathbb{R}^3 \to \mathbb{R}^5$ , what is the minimum amount of information you need to build the standard matrix for the transformation?
- (c) What must a linear transformation do to a line?